

DEVELOPMENT OF A FINITE ELEMENT BASED DELAMINATION ANALYSIS FOR  
LAMINATES SUBJECT TO EXTENSION, BENDING, AND TORSION

BY

STEVEN J. HOOPER  
ASSISTANT PROFESSOR  
DEPARTMENT OF AEROSPACE ENGINEERING  
WICHITA STATE UNIVERSITY  
WICHITA, KANSAS 67208

Delamination is a common failure mode of laminated composite materials. This type of failure frequently occurs at the free edges of laminates where singular interlaminar stresses are developed due to the difference in Poisson's ratios between adjacent plies. Typically the delaminations develop between 90 degree plies and adjacent angle plies.

Edge delamination has been studied by several investigators using a variety of techniques. Pipes, et. al. [1,2] first identified this problem when they predicted the interlaminar stresses in a laminate loaded in tension. O'Brien [3], Raju and Whitcomb [4] analyzed this problem using a quasi-three-dimensional finite element technique. They calculated the fracture toughness of the laminate in addition to calculating the interlaminar stress distributions. Armanios and Rehfield [5] employed an approximate elasticity solution to solve this problem.

Recently, Chan and Ochoa [6] applied the quasi-three-dimensional finite element model to the analysis of a laminate subject to bending, extension, and torsion. This problem is of particular significance relative to the structural integrity of composite helicopter rotors. Such a test would employ a servo-hydraulic tension/torsion machine to apply a twisting moment to O'Brien's EDT specimen [7].

The task undertaken this summer was to incorporate Chan and Ochoa's formulation into Raju's Q3DG program [8]. The resulting program will be capable of modeling extension, bending, and torsional mechanical loadings as well as thermal and hygroscopic loadings. The addition of the torsional and

bending loading capability will provide the capability to perform a delamination analysis of a general unsymmetric laminate containing four cracks, each of a different length.

The solutions obtained using this program will be evaluated by comparing them with solutions from a full three-dimensional finite element solution. This comparison will facilitate the assesment of three-dimensional affects such as the warping constraint imposed by the load frame grips. It will also facilitate the evaluation of the external load representation employed in the Q3D formulation. The external loads are formulated in terms of the twisting curvatures and laminate theory. The resulting load vector in laminate theory is dominated by the twisting moment term. This term appears to violate the natural boundary condition at the free edge of the laminate. This is of particular interest, since these edges contain the cracks, and thus it is this area where stresses must be most accurately modeled. Finally, strain energy release rates computed from the three-dimensional results will be compared with those predicted using the quasi-three-dimensional formulation.

## REFERENCES

1. Pipes, R.B. and Pagano, N.J., "Interlaminar Stresses in Composite Laminates Under uniform Axial Extension," Journal of Composite Materials, Vol 4, 1970, pp. 538-548.
2. Wang, A.S.D. and Crossman, F.W., "Some New Results on Edge Effects in Symmetric Composite Laminates," Journal of Composite Materials, Vol 11, 1977, pp. 92-106.
3. O'Brien, T.K., "Mixed-Mode Strain-Energy-Release Rate Effects on Edge Delamination of Composites," Effects of Defects in Composite Materials, ASTM STP 836, American Society for Testing and Materials 1984, pp. 125-142.
4. Whitcomb, J.D. and Raju, I.S., "Analysis of Interlaminar Stresses in Thick Composite Laminates With and Without Edge Delamination," Delamination and Debonding of Materials, ASTM STP 876, W.S. Johnson, Ed., American Society for Testing and Materials, 1985, pp. 69-94.
5. Armanios, E.A. and Rehfield, L.W., "Interlaminar Fracture Analysis of Composite Laminates Under Bending and Combined Bending and Extension," presented at the ASTM Eighth Symposium on Composite Materials Testing and Design, April 1986.
6. Chan, W. and Ochoa, O., "An Integrated Finite Element Model of Edge Delamination Analysis Due to Tension, Bending and Torsion Loads," AIAA Paper No. 87-0704-CP, 28th AIAA SDM Conference, April 6-8, 1987.
7. O'Brien, T.K., "Characterization of Delamination Onset and Growth in a Composite Laminate," Damage in Composite Materials, ASTM STP 775, Reifsnider K.L., Ed., American Society for Testing and Materials, 1982, pp. 140-167.
8. Raju, I.S. "Q3DG - A Computer Program for Strain-Energy-Release Rates for Delamination Growth in Composite Laminates," NASA CR-178205, Nov. 1986.